

THE INFLUENCE OF SURFACE COATINGS ON THE TOOTH TIP DEFLECTION OF POLYMER GEARS

VPLIV POVRŠINSKIH PREVLEK NA POVES VRHA ZOBA POLIMERNIH ZOBNIKOV

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When designing gear drives made of polymer, the tooth tip deflection is a crucial parameter in respect to the proper gear drive operation. Excessive tooth tip deflection can lead to serious disturbances of gear meshing and consequently to increased noise and wear of the teeth flanks. In such cases the tooth tip deflection can be reduced through the use of stiff surface coatings on the tooth flanks. In this paper the influence of different coating materials and thicknesses on the tooth tip deflection of polymer gears is analysed using comprehensive finite element computational analysis. The numerical results obtained are then used to define an approximate equation for the calculation of gear tooth tip deflection for the coating material used and the thickness of the surface coating layer. The results show that the tooth tip deflection decreases with large values of the coating material Young's modulus and with the coating layer thickness.

Keywords: polymer gears, surface coatings, tooth deflection, numerical analysis

Pri konstruiranju zobniških dvojic s polimernimi zobniki je poves vrha zoba zobnika eden ključnih dejavnikov, ki vpliva na pravilno delovanje zobniške dvojice. Prevelik poves vrha zoba namreč vodi do resnih motenj pri ubiranju zobniške dvojice, kar povzroči večji hrup in tudi večjo obrabo zobnih bokov. V takšnih primerih lahko poves vrha zoba zobnika zmanjšamo z uporabo togih površinskih prevlek. V predloženem prispevku je predstavljena obsežna numerična analiza po metodi končnih elementov, ki zajema vpliv materiala trde prevleke in debeline prevleke na poves vrha zoba zobnika. Numerični rezultati so nato uporabljeni za določitev aproksimativne enačbe za izračun povesa vrha zoba zobnika v odvisnosti od izbranega materiala prevleke in njene debeline. Končni rezultati kažejo, da se poves vrha zoba zmanjšuje z večanjem modula elastičnosti prevleke in debeline utrjenega površinskega sloja zobnih bokov.

Ključne besede: polimerni zobniki, površinske prevleke, poves zoba, numerične analize

1 INTRODUCTION

The primary function of gears is to transmit rotary or linear motion. The design for the kinematics of a gear set is geometrically controlled when the deflections of gear teeth during the gear drive operation are taken into account. Therefore, the selection of appropriate gear material is crucial in the design process. Recently, the development of new materials and technologies have resulted in increased use of engineering polymers for machine elements (e.g. gears) due to benefits such as low cost for injection moulding, light weight, resilience and their ability to operate under dry, unlubricated conditions.¹ Polymer gears, when used in moderate power transmission applications without lubrication may have potentially conflicting tribological properties (low friction, high resistance to wear) and mechanical properties (stiffness, fracture strength). This situation is further complicated by the complex loading and contact phenomena that change throughout the meshing cycle. As the transmissible power levels increase, problems of surface temperatures arise due to the frictional losses between mating gear teeth.^{2,3}

Most of these coatings are based on zinc and aluminium, which are mainly used for radio frequency shielding and electrical conductivity where the mechanical properties of the coatings are not of prime importance. The use of polymer with good strength to weight ratio as a base material is an alternative to metallic components. The main disadvantage is the poor wear resistance of contact surfaces. Recent research work regarding these problems has indicated that thermal spray coatings on polymers can be applied in many engineering applications. Careful selection of material combinations and the use of special process parameters can produce relatively thick metal, ceramic or carbide coatings which can be machined or ground.⁴

It is very important to optimize the gear design before the tools for manufacturing and experimental testing are made to decrease their cost. Traditionally, the gear designer had a limited number of analytical tools as well as his own experience to achieve this goal. Some of the most well known analytical tools for the prediction of gear tooth strength are the procedures according to ISO, VDI and AGMA standards.⁵⁻⁷ As noted earlier, the tooth tip deflection becomes important for gears made of

materials with low stiffness (e.g. polymers) as it can lead to disturbances in gear meshing in the case of excessive tooth tip deflection. The procedure of gear meshing considering the deflection effect is described in the VDI 2736 standard,⁷ where spur gear tooth tip deflection is influenced by the force, tooth face width and material stiffness, which is represented by the Young's modulus and the gear geometrical parameters. It is known that the Young's modulus of polymer materials is much smaller than that of steels, which are often used as gear materials. Furthermore polymer stress-strain behaviour is also affected by changes in the temperature.

Lately, thermoplastic polymers are widely used in manufacturing polymer gears. They have different stress-strain behaviour in the tensile than in the compression region which leads to different values of the Young's modulus in both regions. Furthermore, polymers can also show nonlinear behaviour in the elastic region which cannot be described with a Young's modulus. Therefore, the different stress-strain behaviour in tensile/compression regions and the nonlinear behaviour in an elastic region have to be described with an appropriate constitutive model using an appropriate computational approach (e.g. Finite Element Method). P. Wyluda and V. Wolf¹ performed an elastic-plastic finite element analysis of meshing of two acetal copolymer spur gears under quasi-static loading conditions. Their computational results were in a relative good agreement with the experimental data. The effect of PTFE on the tribological behaviour of polymers in rolling sliding contact has been investigated for two of the most widely used polymers – PA 66 and polyacetal. The experimental results showed that the friction and wear performance of the PTFE filled polymers was superior to that of the unfilled polymers. In addition, the surface cracking found in unfilled PA66 and thought to be responsible for the premature fracture of components such as gear teeth was suppressed by the PTFE. It is suggested that a combination of high surface temperature and high surface tensile stress, produced by friction, is required to initiate these cracks and that PTFE inhibits crack formation by reducing friction.⁸

In general, the gear tooth tip deflection can be decreased using a stiffer material with higher Young's modulus. If a gear is made of low stiffness material (e.g. polymer) the gear tooth stiffness can be increased using a stiff surface coating. Because the standard VDI procedure for the determination of gear tooth deflection includes only homogenous material properties, it is not possible to determine the deflection of a coated gear tooth using the equations available in the above quoted standards.⁷ For this reason, an appropriate computational model to analyse the tooth tip deflection of coated polymer spur gears with different coating materials is presented in this paper.

2 MATERIALS AND METHODS

Polymer materials have low stiffness that can lead to greater deflection of elements made of such materials. Excessive deflection can lead to serious problems in the meshing of polymer gears and consequently the additional loading of the gear teeth. According to the VDI 2736⁷ the deflection of the tooth tip of a spur gear in the circumferential direction can be approximately calculated from Equation (1):

$$\lambda = \frac{\frac{F_t}{b}}{\frac{2E_1 E_2}{c' \cdot \frac{E_1 + E_2}{E_{\text{steel}}}}} \quad (1)$$

where F_t is the tangential force in N, b is the face width in mm, c' is the maximum tooth stiffness per unit face width (single stiffness) of a tooth pair in $\text{N/mm} \times \mu\text{m}^2$, E_{steel} is the modulus of elasticity of steel ($E_{\text{steel}} = 210000$ MPa) and $E_{1,2}$ are the elastic moduli of gears 1 and 2 in MPa at room temperature. The maximum tooth stiffness per unit face width can be expressed in the Equations (2) and (3)⁶:

$$c' = c'_{th} \cdot C_M \cdot C_R \cdot C_B \cdot \cos \beta \quad (2)$$

$$c'_{th} = \frac{1}{q'} \quad (3)$$

Equation (2) uses the theoretical single tooth stiffness c'_{th} as given by Equation (3), where q' is the minimum value for the flexibility of a gear pair. Individual factors in Equation (2) can be determined as described in the ISO 6336 standard: C_M is the correction factor that takes into account the difference between theoretical and actual values for solid disc gears ($C_M = 0.8$ according to the standard ISO 6336); gear blank factor C_R takes into account flexibility of gear rims and webs ($C_R = 1.0$ for a solid disc according to the standard ISO 6336); the factor C_B reflects the influence of deviation from the gear basic rack profile according to standards ISO 6336 and ISO 53.^{6,9}

The deflection of the tooth tip λ determined with Equation (1) must be smaller than the estimated permissible deformation $\lambda_P = 0.07 \cdot m_n$, where m_n is the normal module in mm. Overcoming of the permissible deflection λ_P can lead to serious disturbances of the meshing gear teeth and consequently to higher noise and a shorter service life of the gear pair.⁷

As mentioned above, Equation (1) cannot be used for calculation of the tooth tip deflection of coated gears. Therefore, an appropriate numerical model should be used in that case. The first step in developing a numerical model for the simulation of tooth tip deflection of coated gears was the creation of a numerical model that will yield proper results to be verified by analytical or experimental solutions, or solutions taken from standardised procedures. For this purpose a two dimensional

plane strain model with homogeneous material properties (Hooke's law) and static load was generated. The stress-strain behaviour of the polymer material used in this paper consists of linear and non-linear regions (**Figure 1**). The assumption of using Hooke's law for polymer gears was verified by comparison of the tooth tip deflections based on material models that consider linear elastic material properties.

The static load used in the present model is based on the assumption that the number of loading cycles during the service life of the gear is small and that the gear is used only for partial rotation (e.g. application of the four bar mechanism and for slow motion of the gear rack). This is necessary due to the presence of polymer hysteresis during loading and unloading. If the material is viscoelastic, the path of loading is not coincident with the path of unloading, which occurs when the material changes significantly in volume and is experiencing large deformations. Furthermore, it is assumed that there is enough time for strain recovery and a permanent set effect of the polymer can be neglected.¹¹

An accurate two-dimensional model of the benchmark gear was developed and imported into the ABAQUS software. The contact position of engaging gear tooth flanks was chosen to be on the outer point of single engagement, where the bending load is highest. Contact between engaging teeth was prescribed as a standard surface to surface contact, with the master surface set on the driving gear and the slave surface on the driven pinion gear. Assuming good lubrication, contact interaction was modelled as tangentially frictionless with finite sliding with no adjustments or smoothing between the surfaces. The influence of coating wear during the service life and consequently its influence on tooth toughness and deflection were not considered.

The pinion in **Figure 2a** was fully constrained in the centre bore, while displacements were only constrained in the gear, and the rotations remained free. The load was applied by torque load in the centre of the gear.

The material properties of the pinion were defined as hyper-elastic in the core and as linearly elastic in various coatings. The mesh was generated with CPS4R-type elements with locally controlled element size at tooth flanks (**Figure 2b**) and with at least ten elements in the

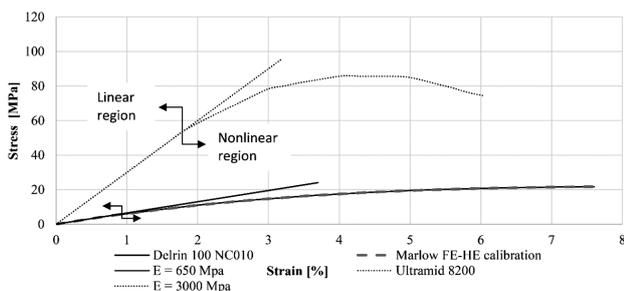


Figure 1: Material properties of pinion core^{10,11,13}

Slika 1: Materialne lastnosti jedra pastorka^{10,11,13}

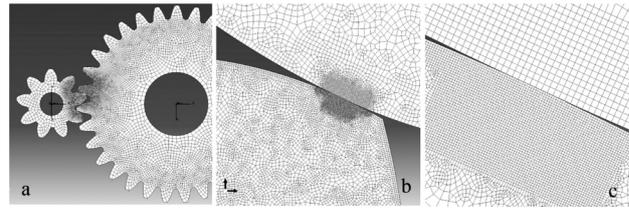


Figure 2: a) Numerical model, b) locally adjusted mesh on gear teeth and c) coating model on pinion

Slika 2: a) Numerični model, b) lokalna zgostitev mreže na zobu in c) prikaz sloja na pastorku

coating layer thickness direction (**Figure 2c**). The numerical model was also tested for convergence analysis. **Figure 3** shows a significant improvement when the number of elements in contact was increased from 467 to 3456. An increase to 5538 elements had no influence on the results or calculation time.

Our workflow was combined from several steps. First, the gear deflection according to VDI 2736⁷ and ISO 6336⁶ standards are calculated. The analysed gears (gear and pinion presented in Table 1) have properties of the steel and the polymer material. Young's modulus and Poisson's ratio for the steel gear was $E = 206000$ MPa and $\nu = 0.33$, respectively, while the polymer material was described with the properties for POM (**Figure 1**) and $\nu = 0.35$. A reference tooth tip deflection was calculated according to Equation (1). In the next step, a model with a coated polymer gear was generated. The pinion gear was partitioned between a coating layer (**Figure 2c**) and core material. Different models were created for different types of coatings and their thicknesses. Two different core material properties from DuPont and BASF (POM Delrin 100 NC010¹² and PA Ultramid® 8202¹³) and several different materials used for coating

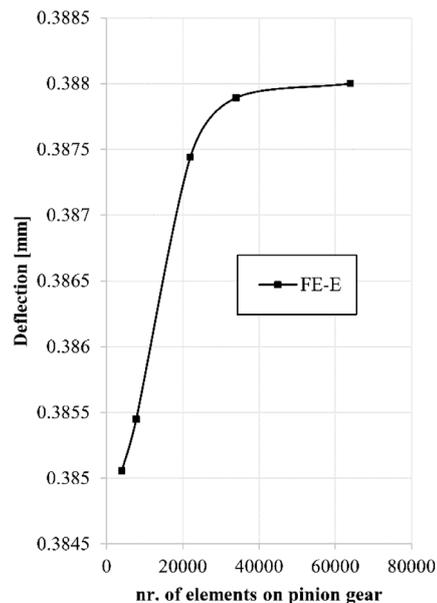


Figure 3: Mesh converge of pinion gear

Slika 3: Konvergenca mreže pastorka

were studied; Polytetrafluoroethylene – PTFE ($E=560$ MPa), aluminium – Al ($E = 70$ GPa), Boron nitride – BN ($E = 33.85– 85.91$ GPa) and Molybdenum disulphide – MoS₂ ($E = 210–400$ GPa) with various Young’s moduli between 560 MPa and 210 GPa.¹⁴ Four different thickness of the coating were modelled on the pinion: $t = 25 \mu\text{m}$, $50 \mu\text{m}$, $75 \mu\text{m}$ and $100 \mu\text{m}$.

Table 1: Details of gear pairs

Tabela 1: Podatki zobniških dvojic

Parameter	Gear pair 1, 2, 3		Gear pair 4, 5	
	Pinion	Gear	Pinion	Gear
Module m (mm)	4		4	
Centre distance a (mm)	80		100	
Pressure angle α (°)	25		20	
Width b (mm)	25	25	25	25
Number of teeth z (-)	9	31	23	27
Profile shift x (mm)	0.4871	-0.4871	0	0
Addendum height h_{aP} (mm)	4.750	2.000	4	4
Dedendum Height h_{fP} (mm)	3.051	6.949	5	5
Root radius profile ρ (mm)	1.24	48	1.83	1.78
Material	POM	42CrMo4	POM/PA	42CrMo4
Young’s modulus E (MPa)	560	206000	560/3000	206000
Poisson’s ratio ν (-)	0.35	0.33	0.35/0.35	0.33

The computational results based on the numerical procedure as described above have then been used to determine the appropriate mathematical formulation where the tooth tip deflection λ is expressed according to the Young’s modulus of the coating material E and the coating thickness t . Several forms of polynomials were used to find the best fit, however the best correlation was found using the following Equation (4):

$$\lambda = A + B \cdot E + C \cdot t + D \cdot \ln t + F \cdot \ln E \quad (4)$$

The computational parameters A , B , C , D and F were calculated using the least squares method. The large value of the coating material’s Young’s modulus and large coating thickness cause a minimum deflection λ , and vice versa. This fact can lead to verification of the model and the derivation of extreme values. Using the global optimization method, the coating material Young’s modulus E and coating thickness t parameters were determined, yielding the minimum and maximum deflections. Equation (4) is valid for general nonlinear elastic base materials.

3 COMPUTATIONAL RESULTS

As described in section 2, the computational analysis of a gear without coating has been carried out first to compare the numerical results with the results of the

analytical procedure as described in VDI 2736.¹⁵ The first finite element analysis (FE-E model) using the standard Young’s modulus and with torque $T = 10$ Nm (tangential force $F_t = 555.6$ N) results in a tooth tip deflection of the uncoated pinion $\lambda = 0.388$ mm, while the standardised VDI calculation gives a value $\lambda = 0.361$ mm. Using a modified computational model (FE-HE model), the tooth tip deflections are also determined for coated gears with different Young’s moduli of coating materials and constant coating thickness $t = 0.1$ mm. As shown in **Figure 3**, the tooth tip deflection of the coated pinion is reduced compared to the tooth tip deflection of an uncoated gear and is for a tangential force, $F_t = 555.6$ N, inside the permissible limit according to VDI 2736. It is evident from **Figure 4** that a reasonably thick coating of $t = 0.1$ mm can have a significant influence on the deflection values of polymer gears.

Combining the computational results with Equation (4), valid parameters for treated Gear pair 1 with regression $R = 0.991$ are determined:

$$A = 0.5173140, B = 8.42502 \cdot 10^{-8}, C = -0.236158, D = 0.000644889 \text{ and } F = -0.0251878.$$

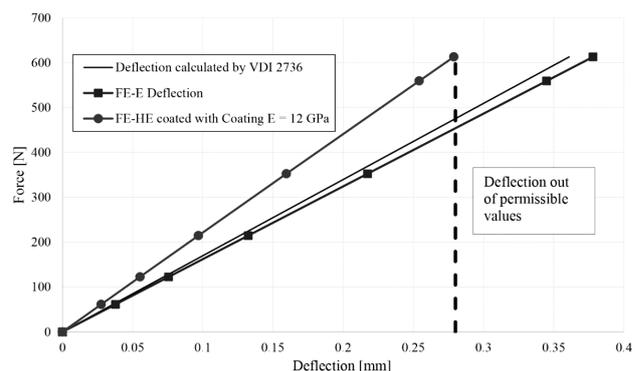


Figure 4: Comparison of gear tooth tip deflection with and without coating (Gear pair 1)

Slika 4: Primerjava povesa vrha zoba zobnika z in brez prevleke (zobniška dvojica 1)

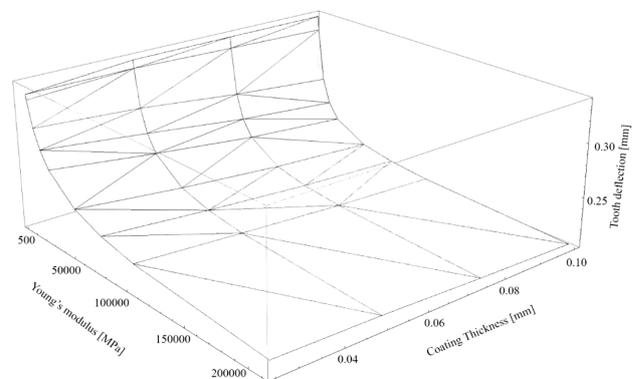


Figure 5: The effect of Young’s modulus and coating thickness on the tooth tip deflection for gear pair 1 and $R = 0.991$

Slika 5: Vpliv modula elastičnosti in debeline prevleke na poves vrha zoba za zobniško dvojico 1 in $R = 0,991$

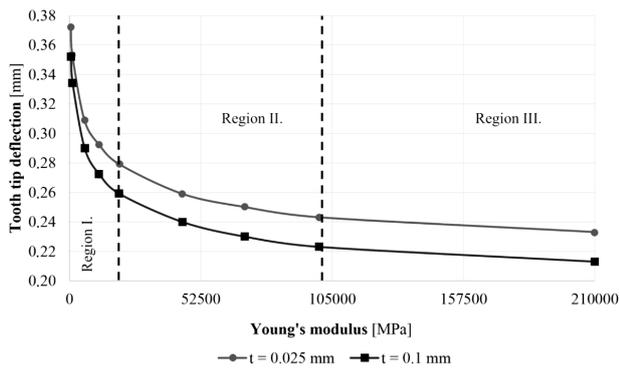


Figure 6: Comparison of tooth tip deflection for two coating thicknesses on gear pair 1

Slika 6: Primerjava povesa vrha zoba za dve debelini prevlek na zobniški dvojici 1

For different gear pairs we obtained the coefficients A, B, C, D, F (Table 3) and with different regression values R which can be found in Table 2. The effect of the Young's modulus E and coating thickness t on the tooth tip deflection according to Equation (4) is presented in Figure 5. The minimum tooth tip deflection $\lambda_{min} = 0.2132$ mm is observed for Young's modulus $E = 210$ GPa and a coating thickness $t = 0.1$ mm, with the maximum tooth tip deflection $\lambda_{max} = 0.3717$ mm seen for Young's modulus is $E = 560$ MPa and coating thickness $t = 0.025$ mm.

The influence of Young's modulus on the tooth tip deflection for minimum ($t = 0.025$ mm) and maximum ($t = 0.1$ mm) coating thicknesses is presented in Figure 6. In region I it can be seen that an increase of the Young's modulus of the surface coating can significantly reduce the tooth tip deflection of the treated gear (about 26.4 % relative to that of Young's modulus $E = 560$ MPa and $E = 20000$ MPa). A somewhat smaller decrease of the tooth tip deflection with increase of Young's modulus is observed in region II (about 13 % relative to that of at $E = 20000$ MPa and $E = 105000$ MPa), while in region III the tooth tip deflection drops only about 6.1 %.

Similar results to those described above are also found when the tooth tip deflection is studied for two given Young's moduli (560 MPa and 210 GPa) and different surface coating thickness (Figure 7). For uncoated gears ($t = 0$) a tooth tip deflection of 0.388 mm is observed. When a surface coating is applied, the significant drop of tooth tip deflection is observed especially for harder surface coatings. In region I (up to coating thickness of 0.025 mm) the decrease of tooth tip

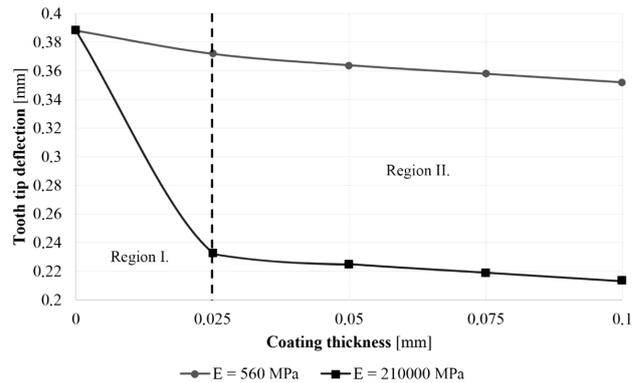


Figure 7: Comparison of tooth tip deflection for two different coating materials on gear pair 1

Slika 7: Primerjava povesa vrha zoba za dva tipa prevlek na zobniški dvojici 1

deflection is about 40 %, while in region II this value is only 9 %.

The deflection behaviour of five gear pairs was examined at the given operating conditions (Table 2). Two distinct geometries were tested with different core materials. Table 2 shows the values for regression of all five cases. The largest deflection has been found in the gear pair 1, with torque 10 Nm and POM as the core material. The smallest deflection was observed in gear pair 5, with torque 10 Nm and PA as a core material.

Table 2: Fitting of equation with FE values

Tabela 2: Ujemanje enačbe z MKE rezultati

Gear	Torque (Nm)	Material	Regression R
Gear pair 1 $i = 9/31$	10	Delrin 100 NC010	0.9910
Gear pair 2 $i = 9/31$	5	Delrin 100 NC010	0.9806
Gear pair 3 $i = 9/31$	1	Delrin 100 NC010	0.9790
Gear pair 4 $i = 23/27$	10	Delrin 100 NC010	0.9781
Gear pair 5 $i = 23/27$	10	Ultramid® 8202	0.9650

In Table 3, the A, B, C, D and F coefficients are given for different gear pairs. It is evident that by reducing force or increasing the stiffness of the base material (gear pair 5), these coefficients approach zero. This is a direct consequence of the fact that the tooth tip deflection decreases with stiffer materials and/or reduced

Table 3: Equation coefficients for equation 4

Tabela 3: Koeficienti za enačbo 4

Gear	A	B	C	D	F
Gear pair 1 $i = 9/31$	0.5173140	8.42502E-08	-0.236158000	0.000644889	-0.025187800
Gear pair 2 $i = 9/31$	0.2407840	3.56586E-08	0.053658500	-0.004475320	-0.012522600
Gear pair 3 $i = 9/31$	0.0463095	7.10510E-09	0.000250842	-0.001774000	-0.002599930
Gear pair 4 $i = 23/27$	0.1549290	3.23817E-08	-0.009230920	-0.006828120	-0.010816000
Gear pair 5 $i = 23/27$	0.0304427	-1.67453E-08	-0.009067370	-0.000983624	-0.001365980

torque. For gear pair 1 (the weakest material and the largest torque) the maximum coefficient deviations and consequently the highest tooth tip deflection was observed.

4 CONCLUSION

The influence of different coating materials and coating thicknesses on the tooth tip deflection of polymer gears made of POM and PA is presented in this paper. The tooth tip deflection was determined numerically using a finite element model. Here, the mechanical properties of the core material were defined using the Marlow hyperelastic material model while the coating materials' mechanical properties were defined using the linearly elastic Hooke's law. The computational results obtained have then been used to define the approximate analytical equation, where linear and logarithmic terms of Young's modulus and coating layer thickness were used. The obtained analytical equation form describes the tooth tip deflection. It is valid for coating material Young's moduli in the range from 560 MPa to 210 GPa, coating thicknesses between 0.025 mm to 0.1 mm, different loads, different nonlinear elastic base materials and different geometries. The final results showed that the use of stiff surface coatings on polymer gears significantly reduce the tooth tip deflection and consequently improve the operation of such gear pairs.

Further investigations for coated polymer gears should cover the potential cracking of hard coatings in the case where the core material stiffness is too low. The coating layer wear due to the relative sliding of gear flanks and its influence on the tooth tip deflection should also be studied. To confirm the computational results, the experimental testing of bending behaviour of coated polymer elements should be carried out.

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